

# SUBTRACTIVE SYNTHESIS

# Introduction

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## Subtractive synthesis

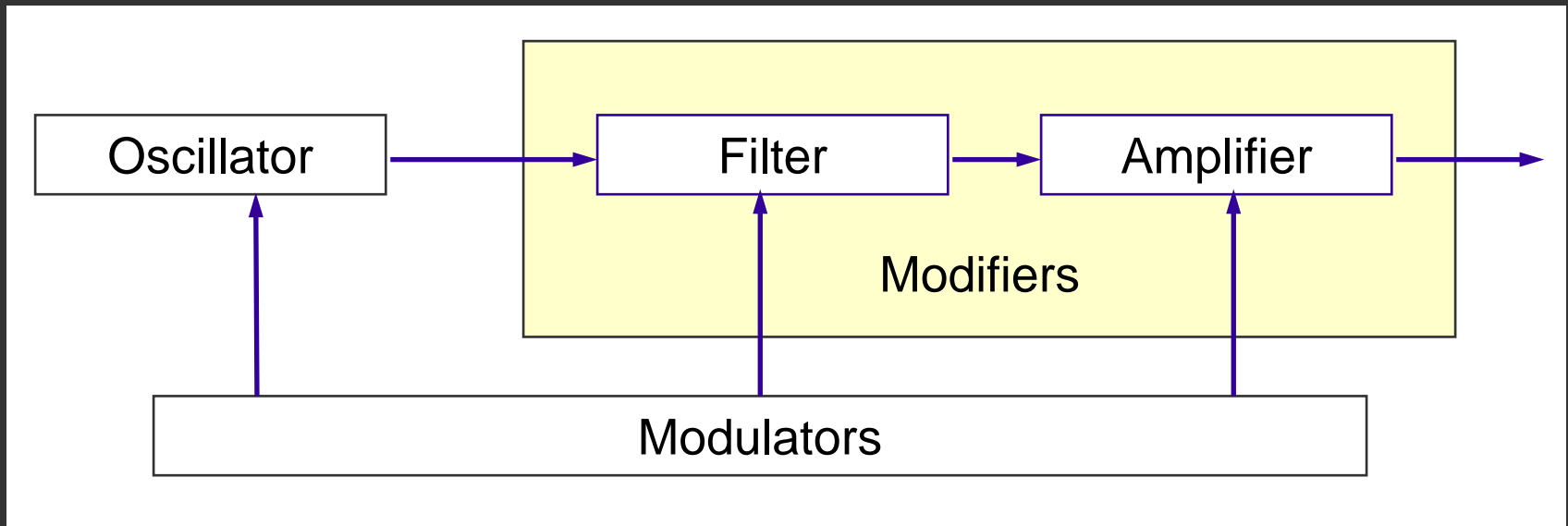
- From Latin *subtractio*
- First synthesis method.
- Also called analogue or modular synthesis.
- For many musicians, “\*the\* synthesis”.
- Originally analogue method, still used in digital instr.
- The main concept:
  - **oscillators** create rough harmonic signals,
  - **filters** shape the static spectrum,
  - **modulators** introduce dynamic changes to the sound.

# Source and modifier

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The subtractive synthesis works on a “source-modifier” basis:

- source - oscillators
- modifiers – filters and modulators



# Source and modifiers

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	Guitar	Synthesizer
Source	Vibrating string	Signals from oscillators
Modifier	Resonant body	Filters
Modulation	A way of picking and pressing strings	Modification of the module parameters

# Oscillators - VCO

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## VCO – Voltage Controlled Oscillator

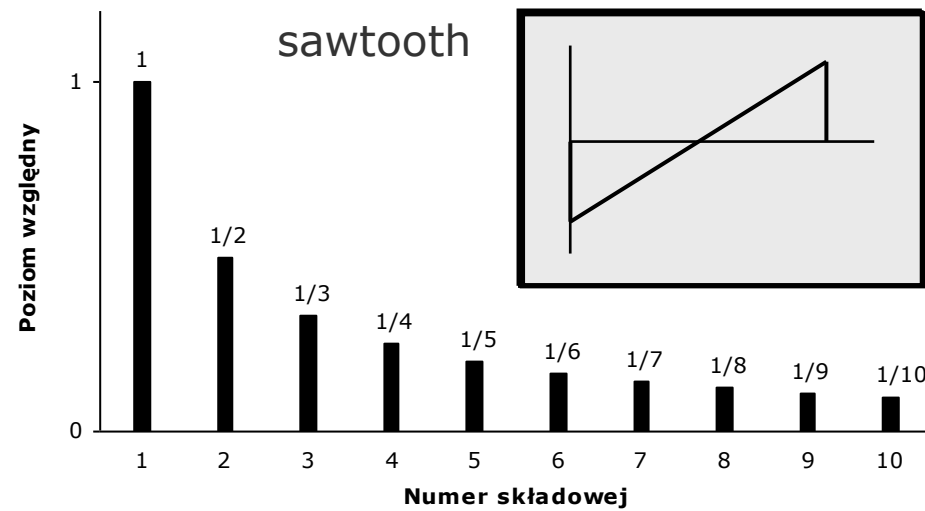
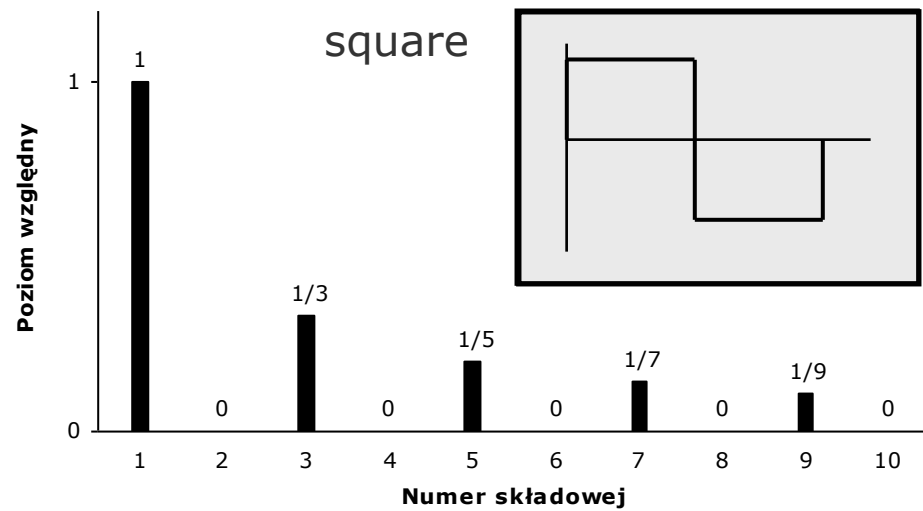
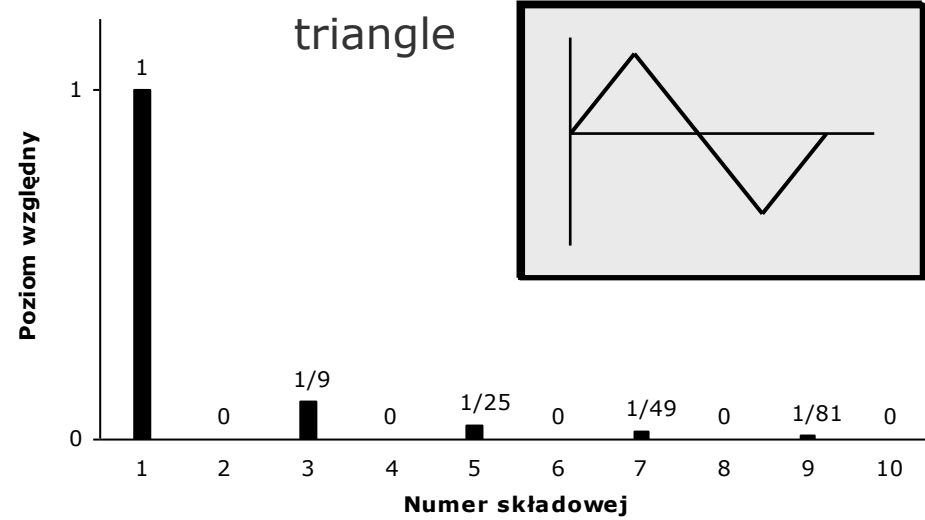
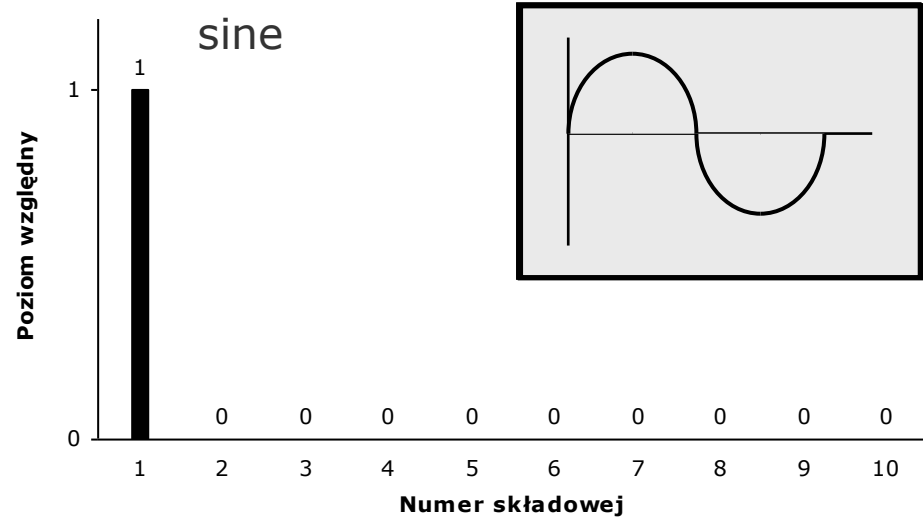
Generates harmonic signals.

A classic VCO generates the following signals (waves):

- sine wave
- triangle wave
- square (rectangular) wave
  - regulated pulse width
- sawtooth wave

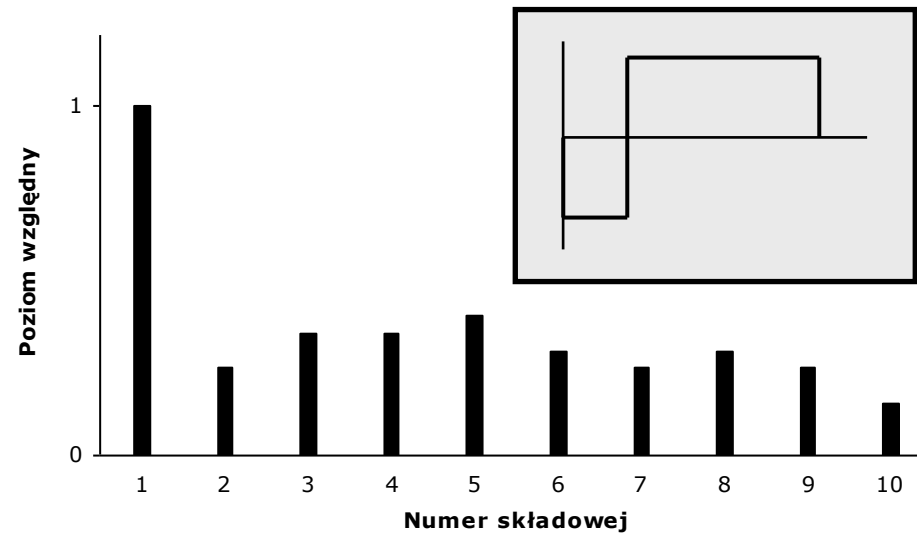
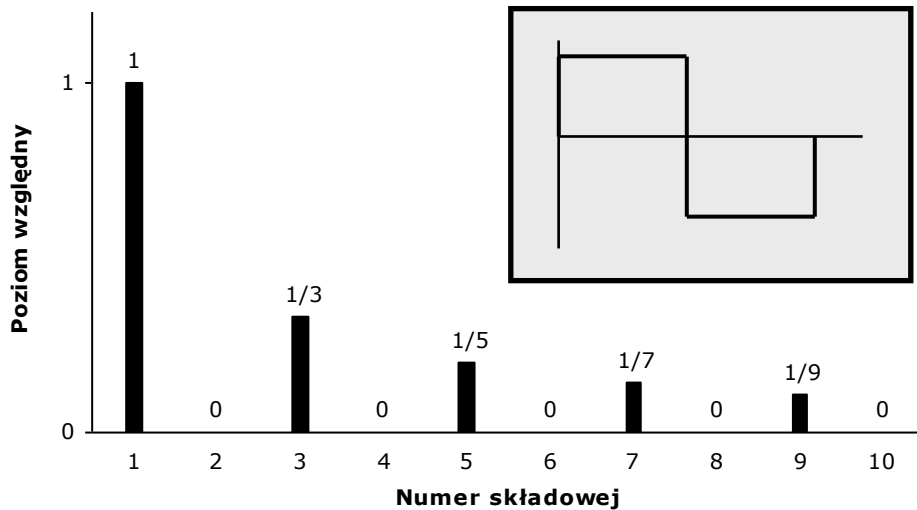
Modern VCOs can also generate more complex waves.

# Simple waves from VCO



# Simple waves from VCO

Square wave can have different shape according to the **pulse width** or **fill rate** parameter (PWM, p/m).



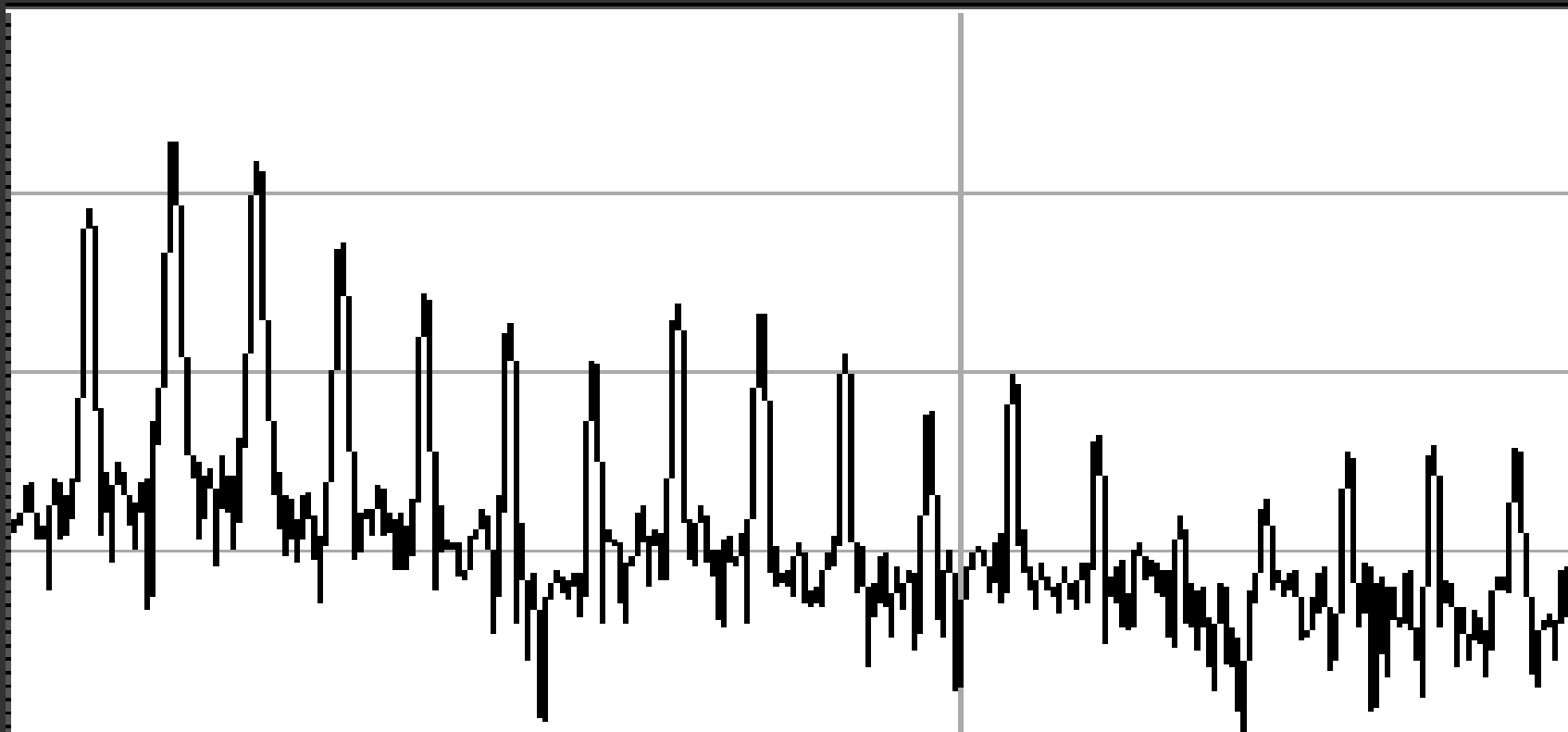
For fill rate 1:1, only odd numbered peaks are present.

Changing the fill rate from 1:1 increases level of even peaks and decreases level of odd peaks.

# Spectrum of a musical sound

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Haven't we seen such a spectrum shape before?

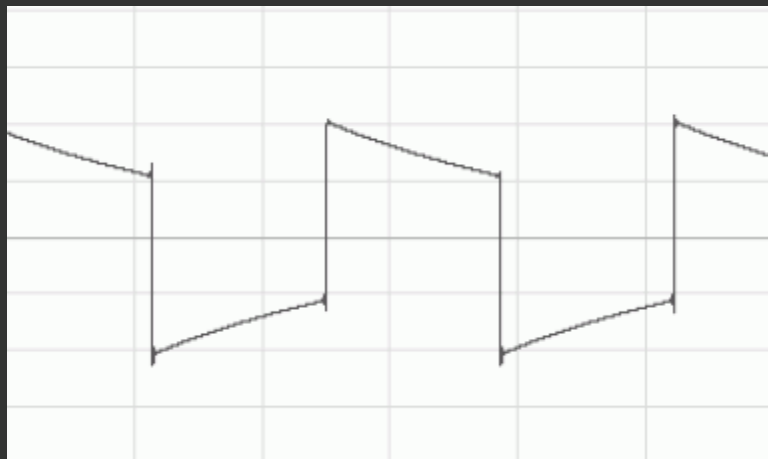
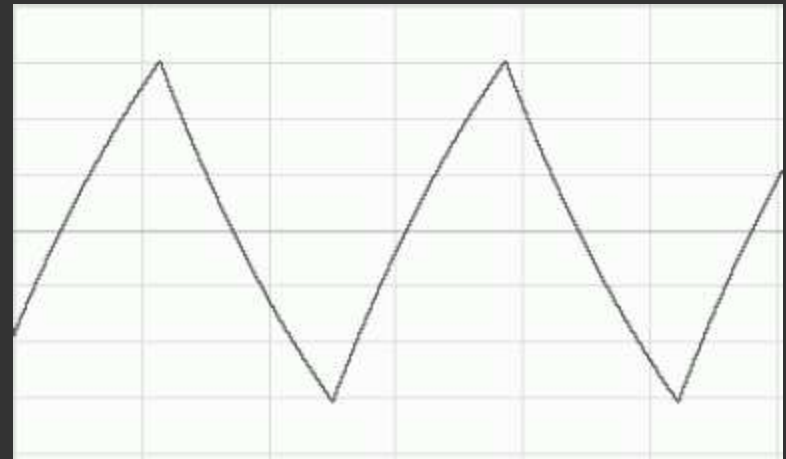
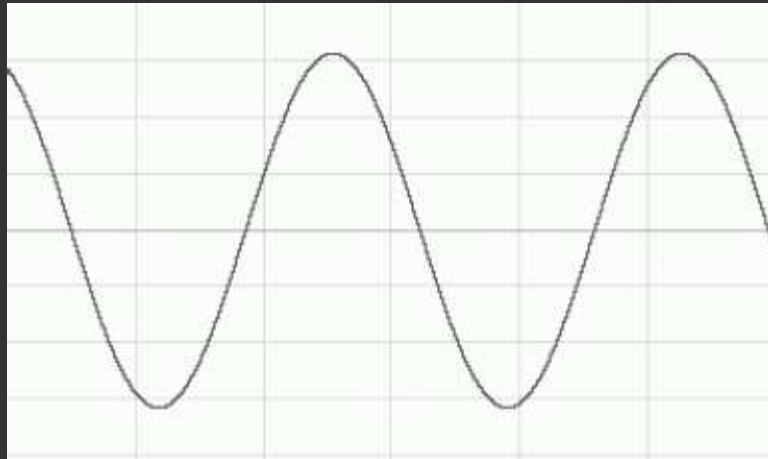




# Waves generated by real analogue VCOs

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Real waves from analogue *Moog Modular*



# Voltage controlled modules

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What does „*voltage controlled*“ mean?

**Voltage control** (VC) means that the parameters (e.g. wave frequency, fill rate) depend on the **voltage of a control signal**.

Where does this control voltage come from?

- From keyboard (changing the sound pitch).
- From knobs on the front (e.g. detuning).
- From a signal generated by another module (the **modulator**), connected to the **control input**.

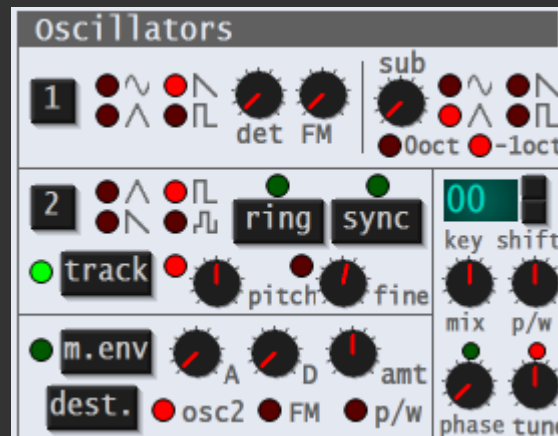
# Oscillator VCO

## Parameters of the VCO:

- wave shape (signal type)
- frequency (detuning)
  - coarse – by octaves,
  - fine – by cents
- fill rate (square wave only)

## Modulation inputs:

- frequency
- fill rate

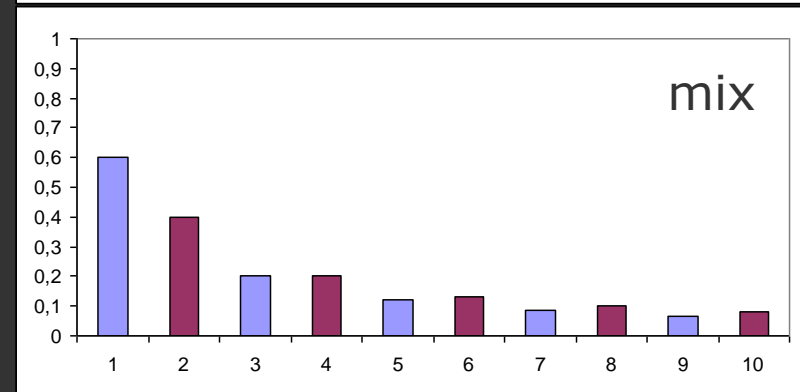
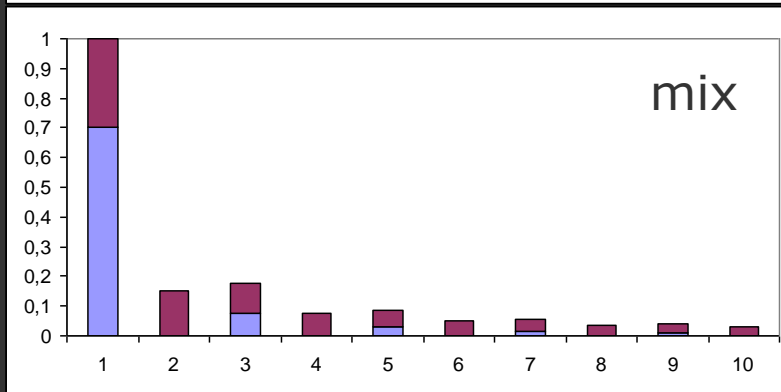
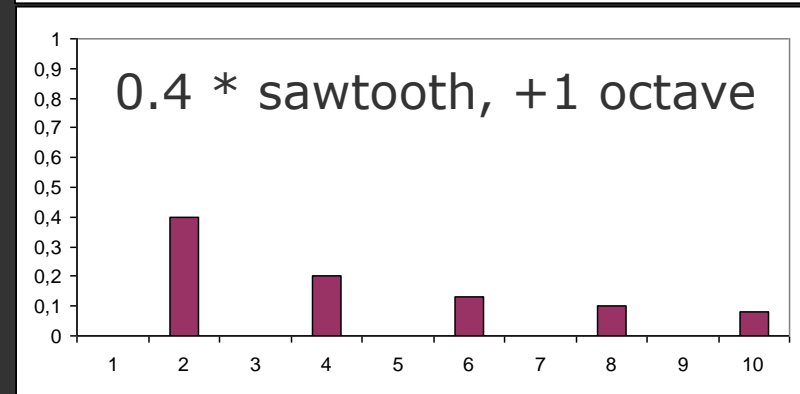
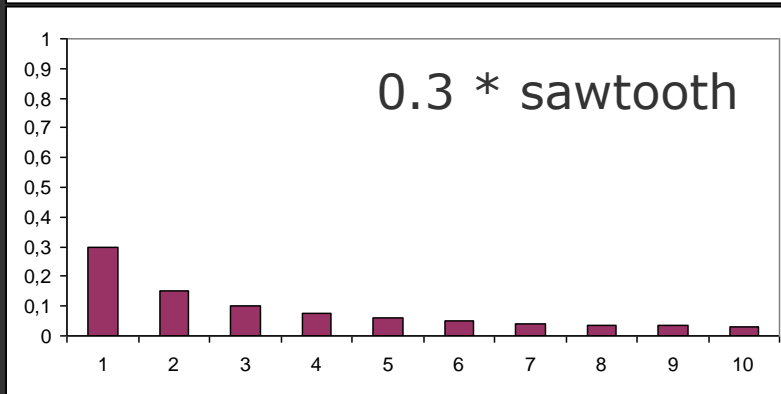
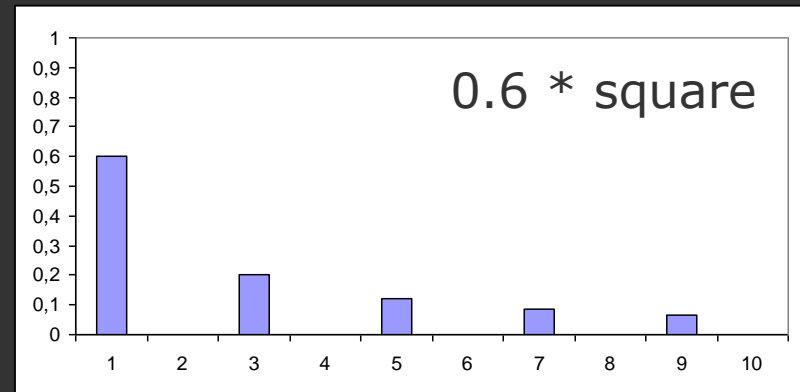
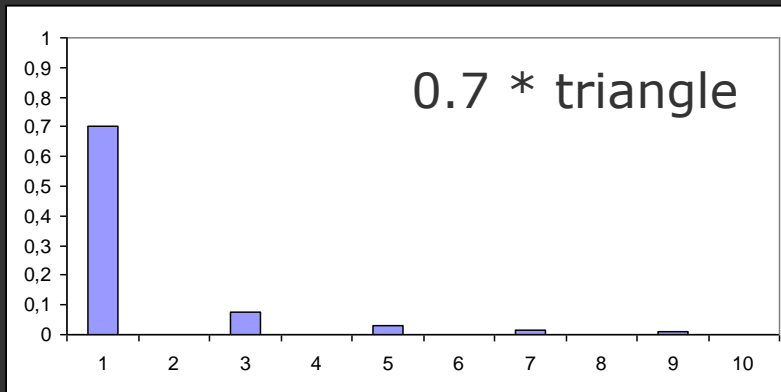


# Multiple oscillators

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- One oscillator is not enough. In practice, waves generated by 2-3 oscillators are summed up (mixed).
- Proportion of the mix can be regulated.
- Some common examples:
  - different wave shapes, same frequency,
  - one wave detuned by one or more octaves, up or down,
  - one wave slightly detuned (the beating).
- With this method, we can shape the spectrum of the initial sound and make it less regular.

# Multiple oscillators



# Multiple oscillators

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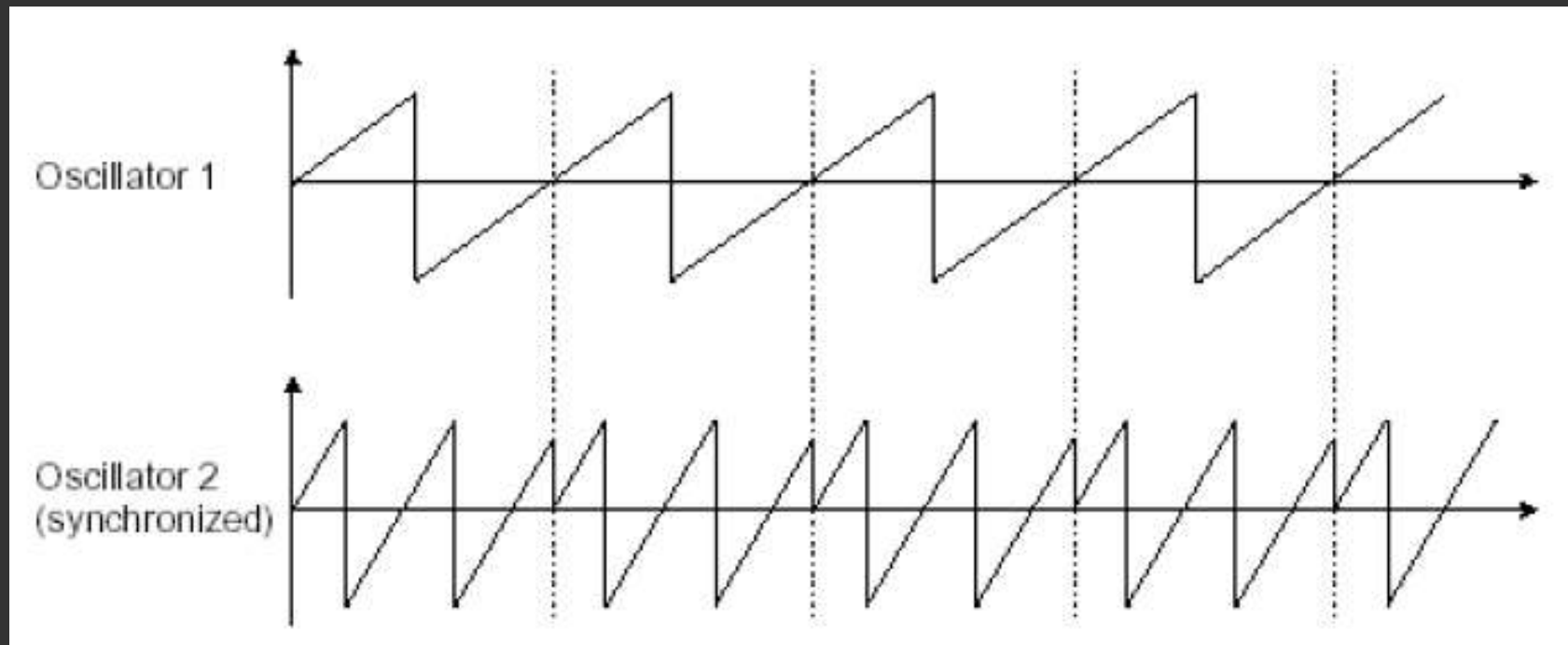
More advanced examples:

- **frequency modulation** (FM) – frequency of VCO1 is modulated by output of VCO2; generates signals with complex spectrum;
- **ring modulation** – signals from VCO1 and VCO2 are multiplied, creating rich, inharmonic sounds,
- **sync** – each new period of wave from VCO1 resets the phase of VCO2, allowing for creation of new wave shapes.

# Oscillator sync

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VCO1 syncs VCO2: resets the phase of VCO2 at the start of each new period in VCO1 signal.



# Filter - VCF

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## VCF – Voltage Controlled Filter

Modifies spectrum of the generated signal.

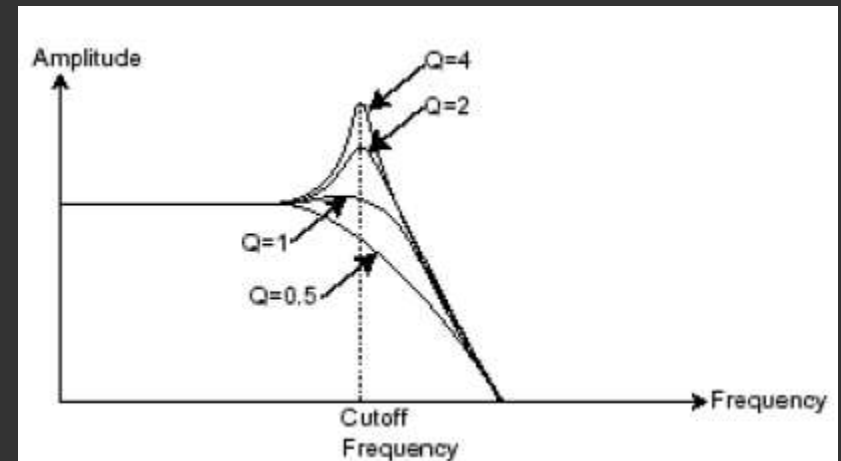
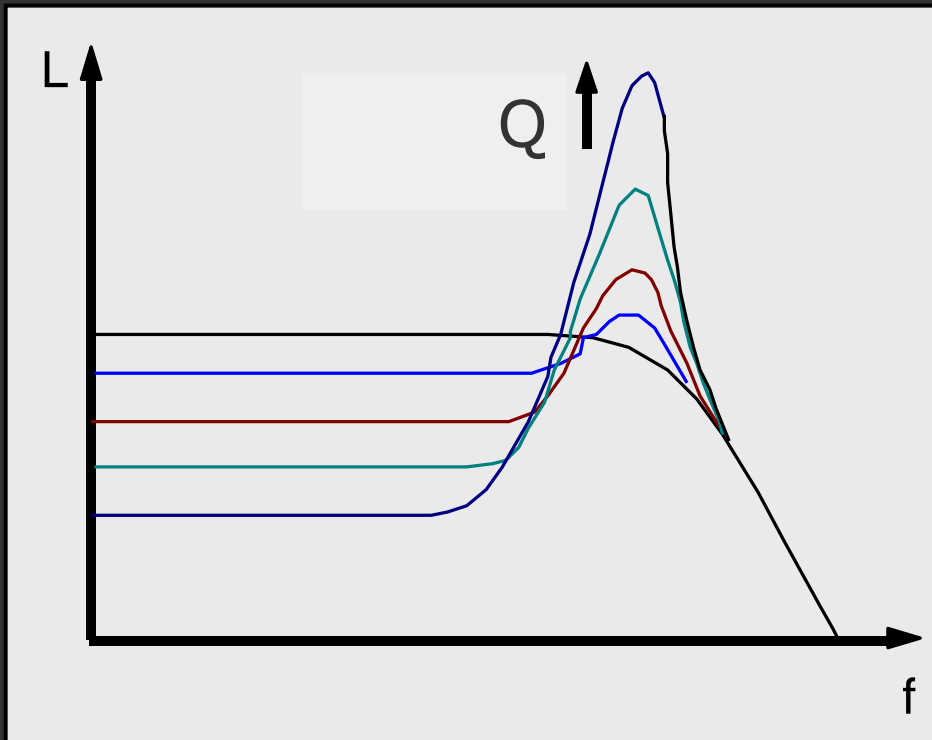
- **Dampens** selected frequency range, defined by a **cut-off** frequency.
- Filters may be: low-pass, high-pass, band-pass.
- Attenuation rate – how quickly the gain falls, usually: 12, 18 or 24 dB/octave.
- **Resonance** (emphasis, Q) – peak near the cut-off frequency, created by a feedback loop in the filter.



# VCF - sample responses

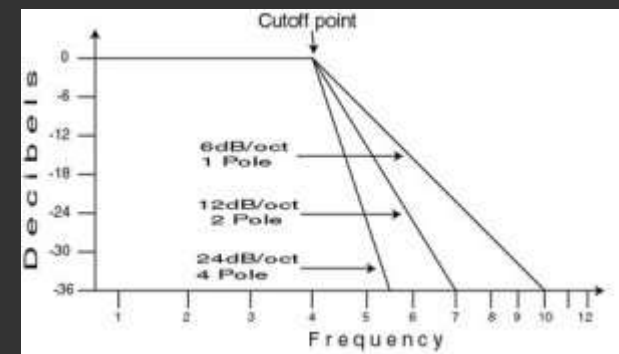
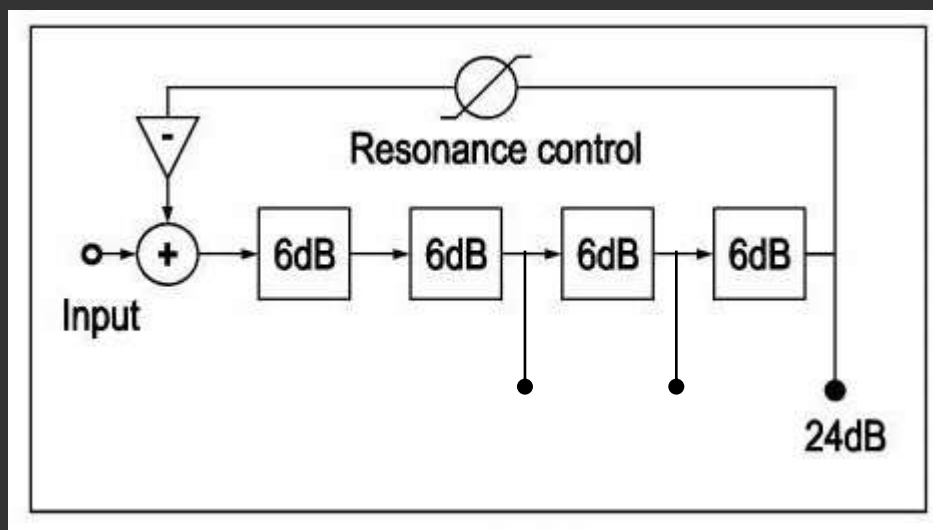
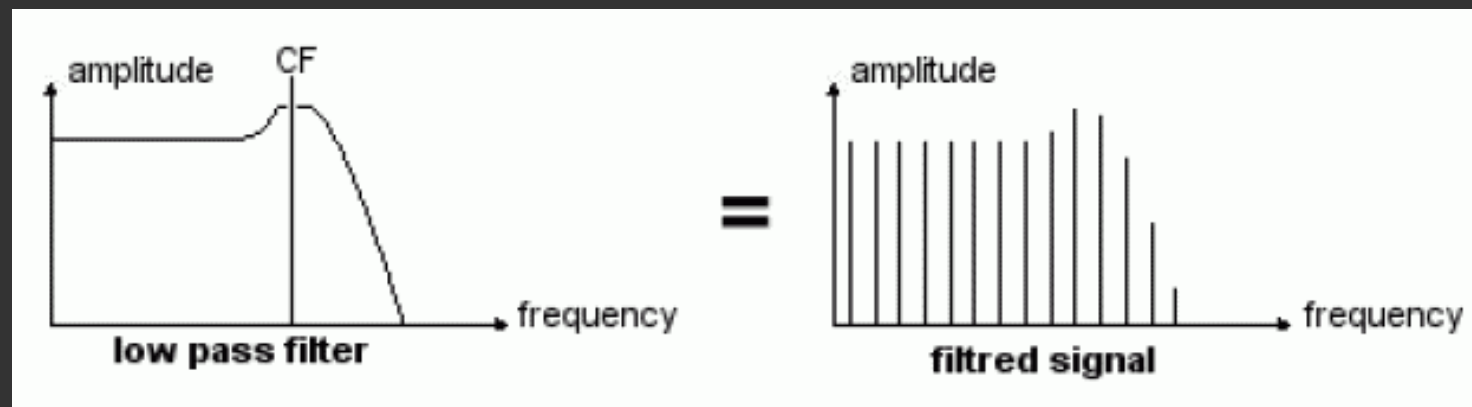
Lowpass filter – the most common type used in synthesizers.

- $Q$  – resonance
- *cutoff* – beginning of the stop band



# Attenuation rate

Attenuation rate defines the range of modified frequencies.

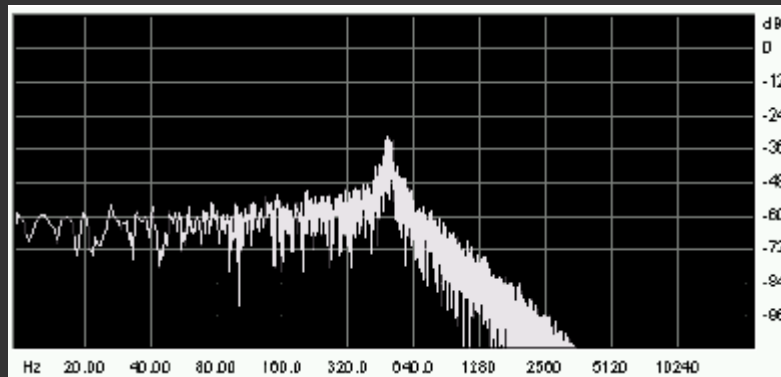


# VCF - filtered signals

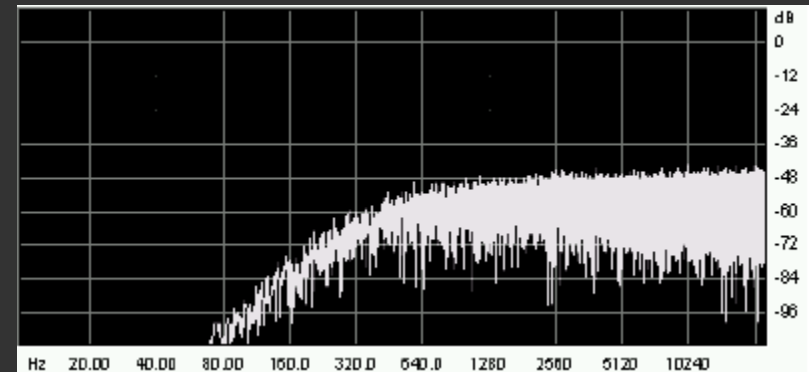
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## Spectra of filtered white noise (Moog Modular)

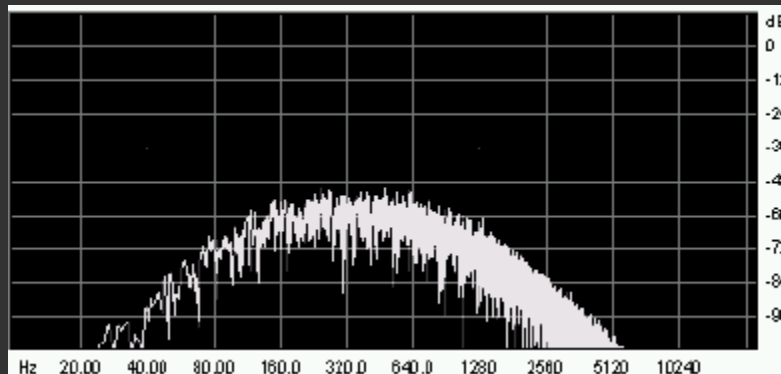
**LP** (low-pass)



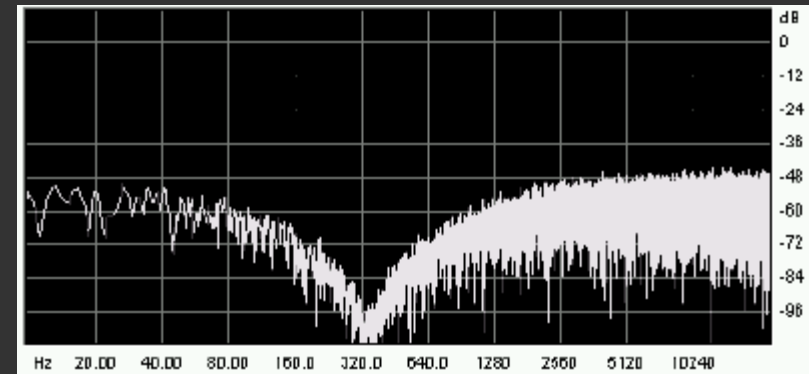
**HP** (high-pass)



**BP** (band-pass)



**BR** (band-stop)



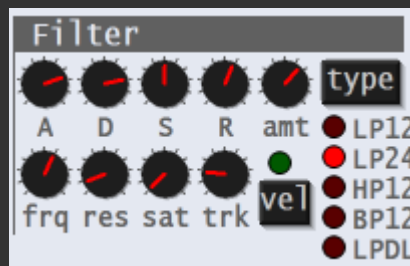
# VCF - filter

## Parameters of VCF:

- filter type
  - LP, HP, BP, *notch* (BS)
- cut-off frequency
- resonance (Q, *res*)
- attenuation rate

## Modulation inputs:

- cut-off
- resonance (rarely)



# Keyboard follow

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*Key follow* allows controlling the module parameters with a musical keyboard. The effect depends on the key number.

If we set a fixed cut-off frequency in VCF, e.g. 2.6 kHz in a low-pass filter, then:

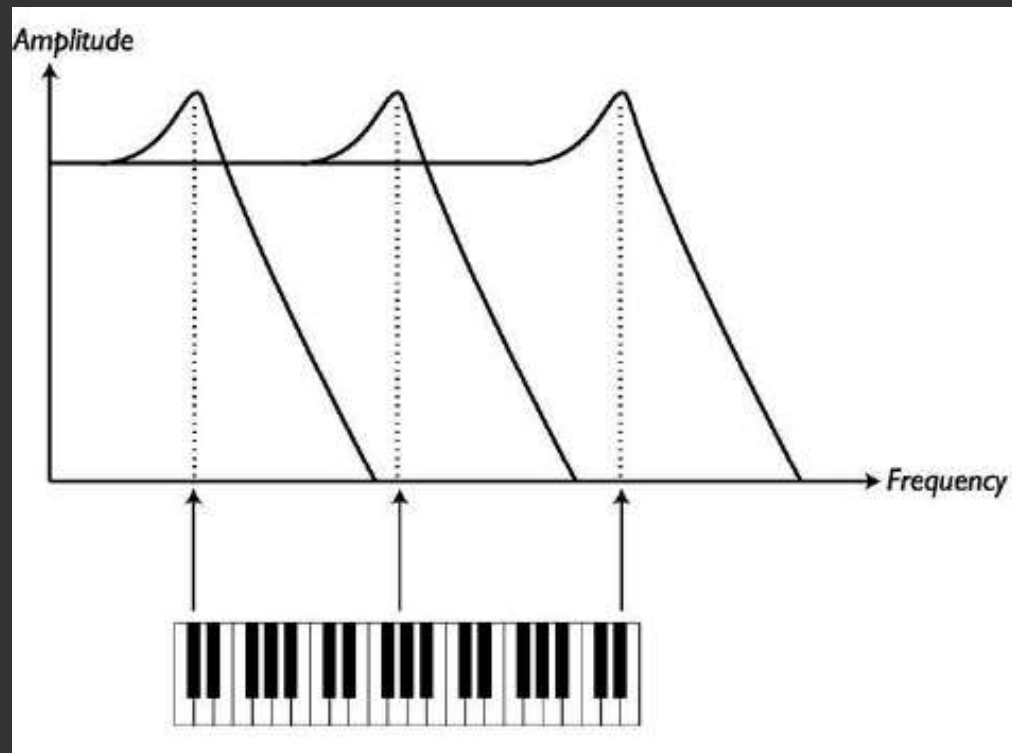
- for a sound with frequency 500 Hz – first 5 partials will be passed through,
- but for a sound with frequency 4 kHz, all partials will be attenuated (they are in the stop band).

This is usually not what we need. We want to attenuate e.g. from 5<sup>th</sup> partial onwards, independently of the fundamental frequency of the signal.

# Keyboard follow

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- With key follow, the cut-off frequency follows the pressed keys. Strength of this effect can be regulated.
- As a result, the timbre of the sound remains constant.
- Similarly, we can apply key follow to other parameters.



# VCA - amplifier + envelope generator EG

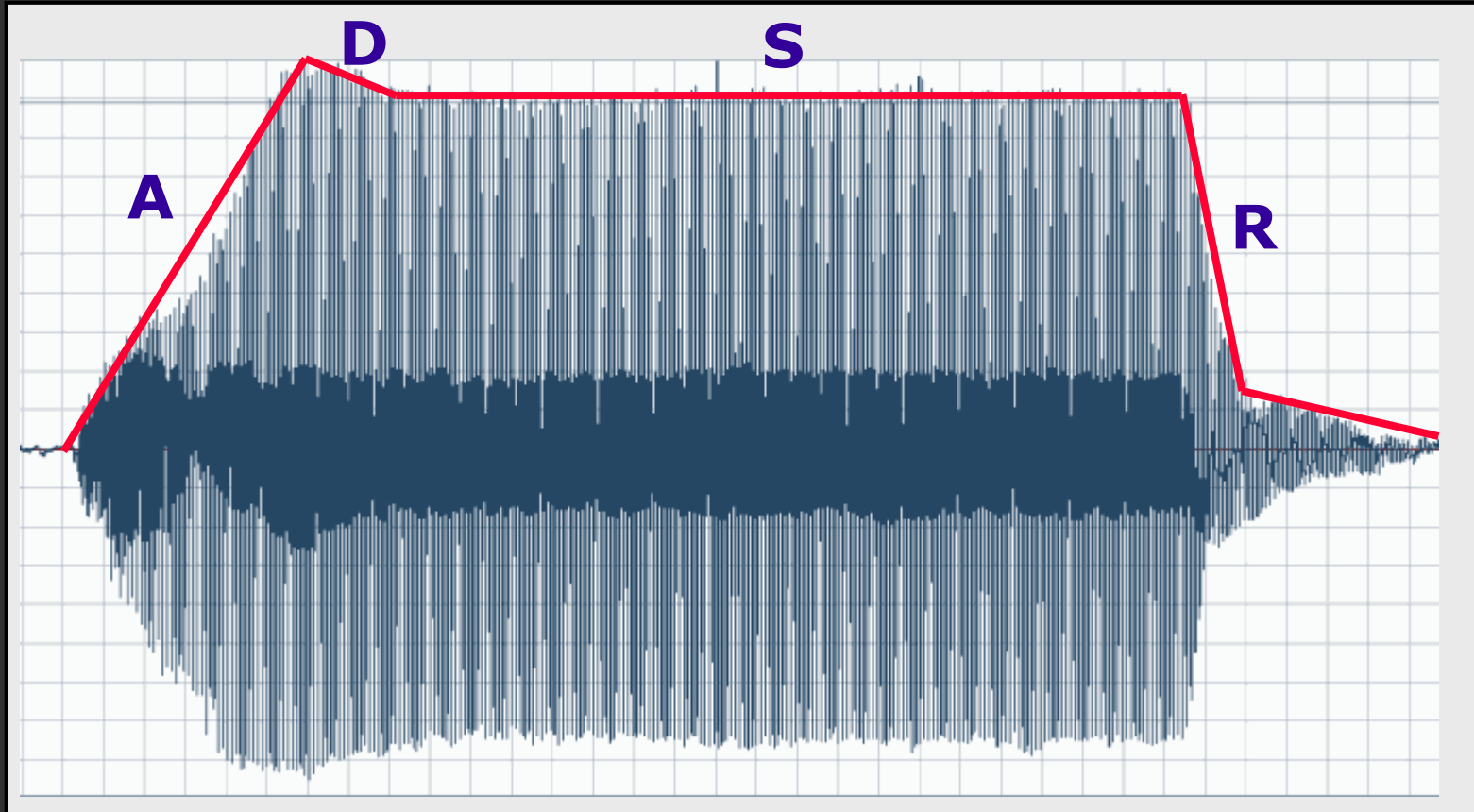
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## VCA – Voltage Controlled Amplifier

- The output module of the synthesizer.
- In practice, VCA is always coupled with an **envelope generator EG** in order to shape the signal envelope.
- EG controls the gain of VCA, according to the **envelope** – a “gain vs. time” function.

# Envelope of a musical sound

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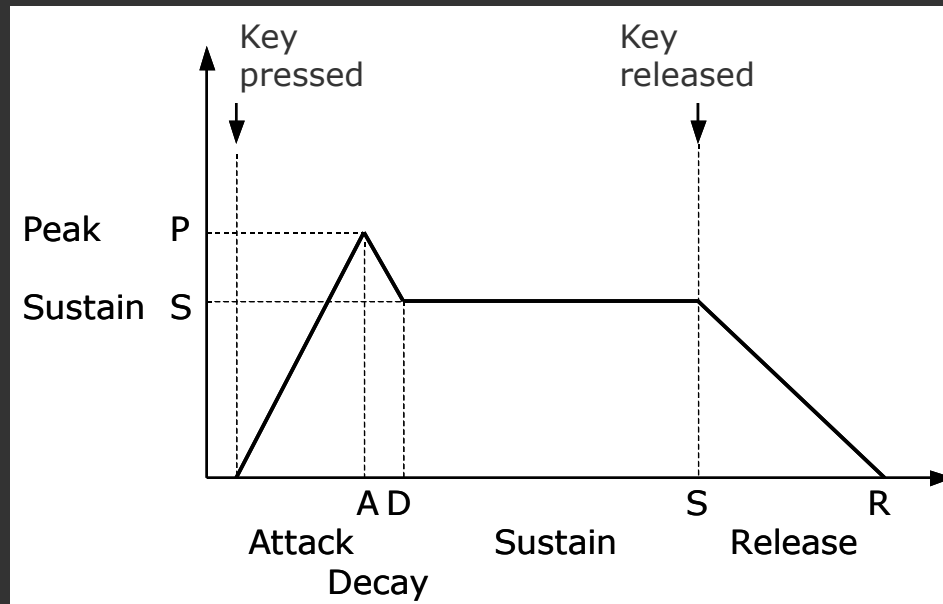


# ADSR envelope

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Parameters of the ADSR envelope:

- **A**: duration of the attack phase
- **D**: duration of the decay phase
- **S**: level of the sustain phase (not duration!)
- **R**: duration of the release phase

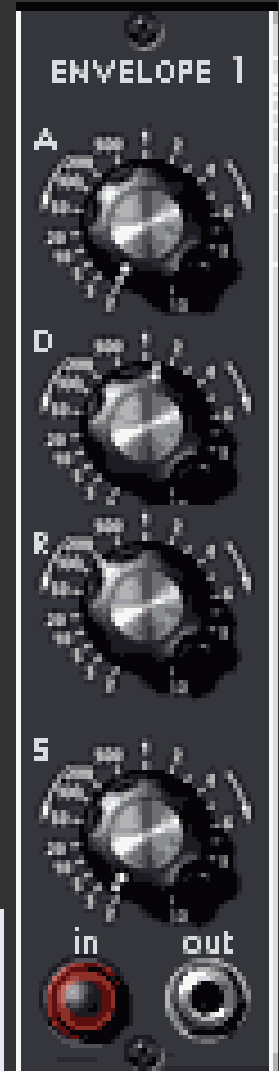
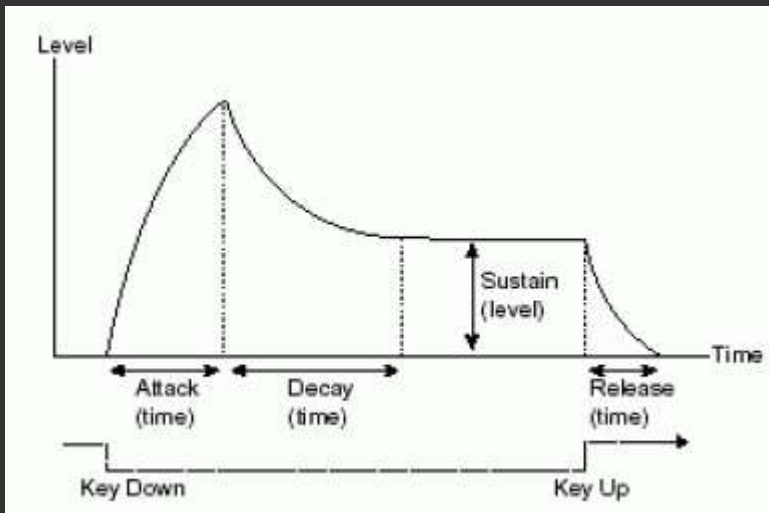


# EG - envelope generator

## EG – envelope generator in VCA

modifies changes of the signal loudness in time.

The ADSR envelope consists of four sections that change linearly or exponentially.



# EG - practical envelope examples

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Sound of a wind instrument (e.g. a trumpet):

- A, R – sufficiently large
- D – is present, but it's short
- S – level slightly below the peak

Sound of a string instrument (e.g. a guitar):

- A – very short
- D – very long
- S – level at zero
- R – zero, or the same as D
- key release should not break the D phase

# Velocity control

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- All professional musical keyboards are **dynamic**, they have **velocity** sensors that measure the “strength” of key pressing.
- Usually, velocity value is used to control the gain of VCA (softer or louder sound for softer or harder key press).
- We can use the velocity to control other parameters, e.g. VCF cut-off (timbre changes according to the strength of key press).



# Modulation

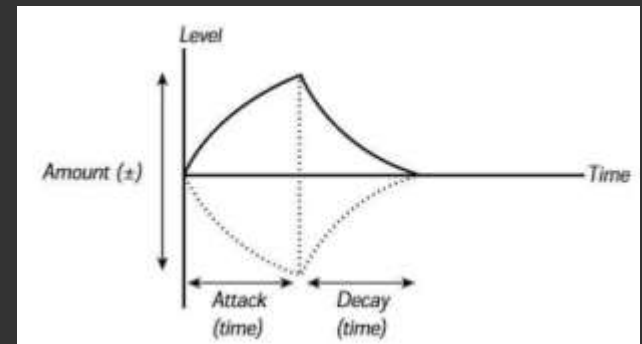
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- Synthetic sounds generated by VCO + VCF + VCA are **static**, their timbre is constant. Hence, they sound dull.
- If we want **dynamic**, alive sounds, we must modify the sound as it plays.
- **Modulation** in sound synthesis is achieved by **changing the control parameters** (voltage) with **control signals**, produced by:
  - envelope generators EG – linear changes,
  - LFO modules – cyclic changes
- Please remember: it is the modulation that makes the subtractive synthesis sound interesting!

# EG is the modulator

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- Envelope generator is an example of a modulator. It produces a control signal (not a sound).
- EG signal can control other modules.
  - VCO envelope – changes the produced frequency. It can be used to modify the attack phase or to create special effect sounds. VCO envelope often has a simplified AD shape.
  - VCF envelope – modifies the cut-off frequency. It may be used e.g. to alter the timbre during the attack phase.

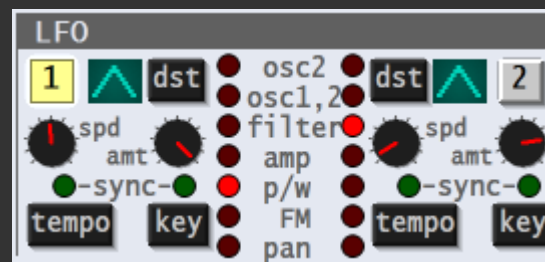


# LFO - low frequency oscillator

**LFO** – Low Frequency Oscillator. Produces **control** (inaudible) signals with frequency below 20 Hz. Otherwise, it is a standard oscillator (similar to VCO).

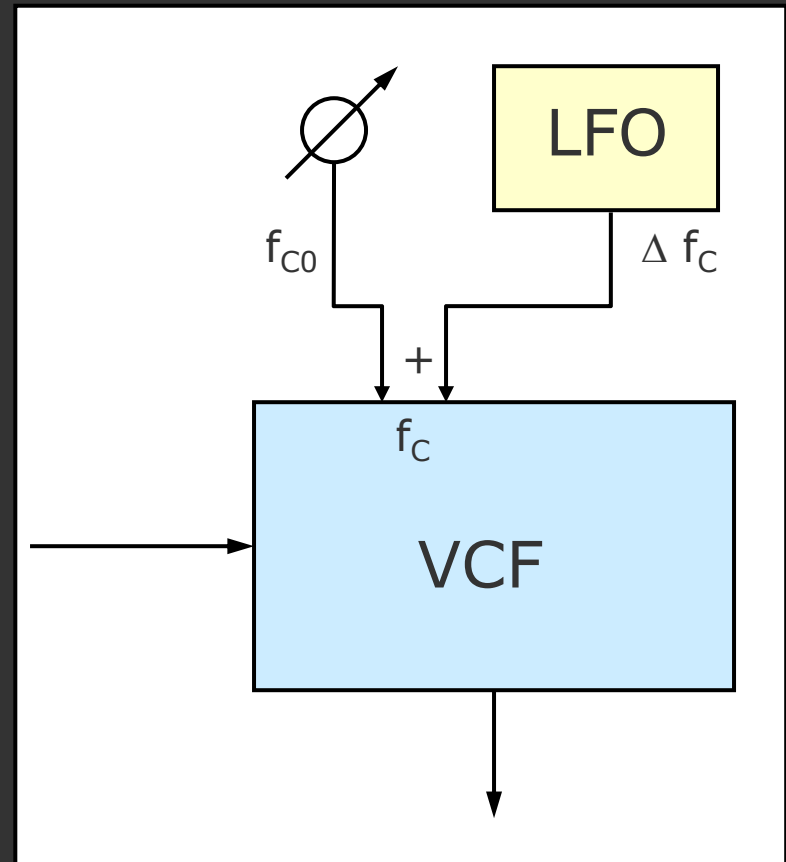
LFO parameters:

- wave shape
- frequency – modulation **rate**
- amplitude – modulation **depth**



# LFO - examples

A typical example: LFO controls the cut-off frequency of VCF. It produces cyclic timbre changes (dark-bright), often called a **sweep**.





# LFO - examples

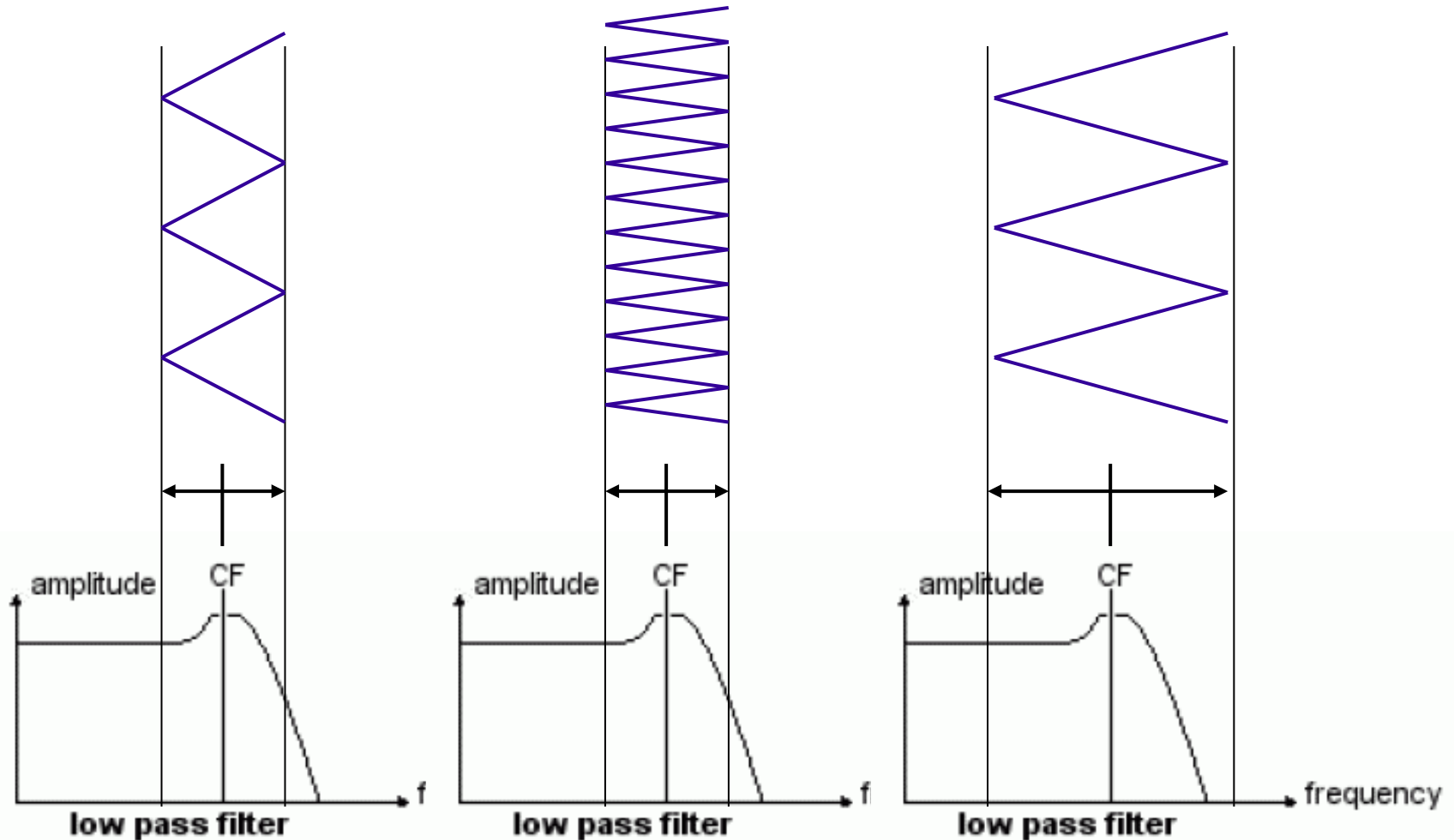
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Modulation parameters:

- LFO waveshape – type of changes (sine or triangle – smooth, square – step, sawtooth - mixed),
- LFO **frequency** – **rate**, how quickly the timbre changes,
- LFO **amplitude** – **depth**, range of timbre changes.

If the amplitude is set too high, a tremolo effect is produced. In extreme cases, the sound may periodically fade out completely (the cut-off reaches zero).

# LFO - cut-off modulation



Higher rate  
(LFO frequency)

Higher depth  
(LFO amplitude)

# Which parameters can LFO modulate?

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VCO:

- signal frequency (vibrato)
- fill rate of a square wave (timbre modulation)

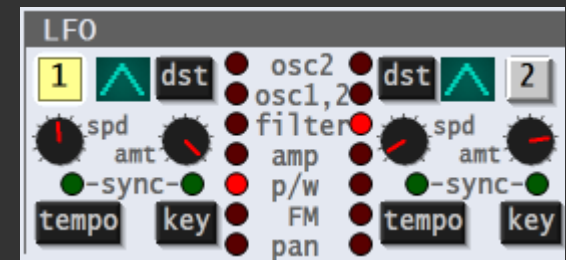
VCF:

- filter cut-off (timbre modulation)
- resonance (rarely available)

VCO:

- output gain (tremolo)
- stereo panning

All module parameters that have control input may be modulated by LFO and EG.



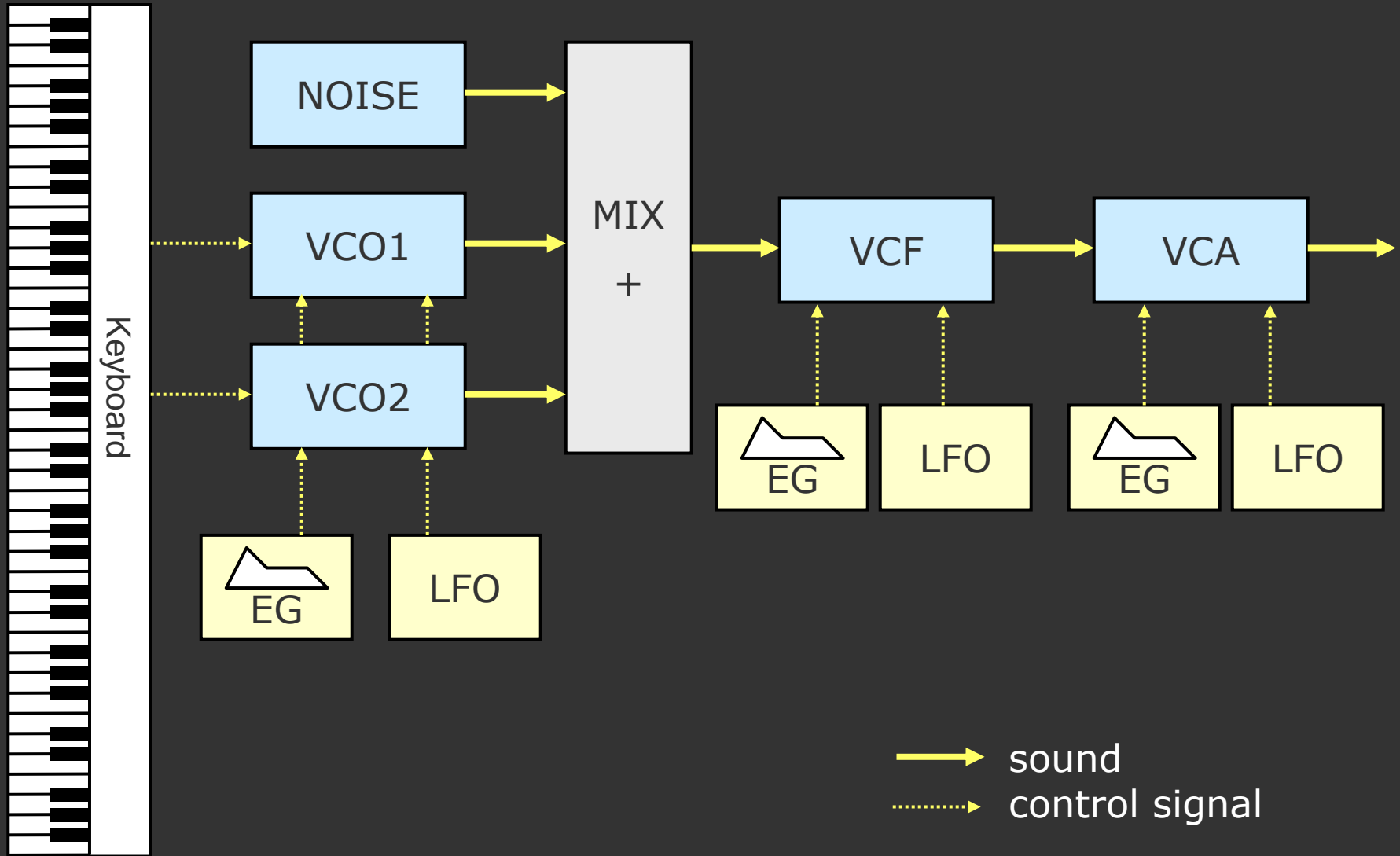
# Modular synthesizer

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A hardware subtractive synthesizer may have two forms:

- modules connected with patches (cables) by a musician (Moog Modular, EuroRack) – more work needed, but much more flexible, a musician creates the synthesis algorithm by himself
- fixed connections between modules (MiniMoog, the majority of modern synthesizers) – easier to use, less flexible, but a standard setup (2-3×VCO, VCF, VCA, EGs, LFOs) is often sufficient.

# General diagram of a subtractive synthesizer



# Additional modules

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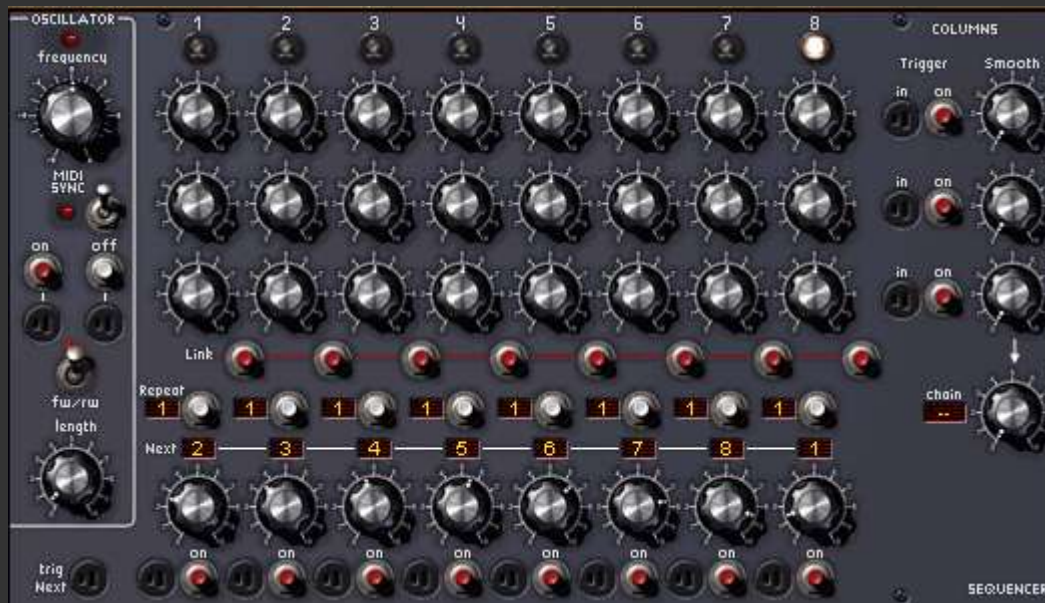
Other synthesizer modules (not present in some instruments):

- sound effects (delay, chorus, phaser, etc.)
- noise generators (RNG – Random Noise Generator)
- sequencer
- arpeggiator
- trigger modules
- sample and hold
- envelope follower
- and others

# Sequencer

Step sequencer:

- generates programmed control sequences
- plays sounds automatically
- triggered by a keyboard or by a square wave generator



# Controlling the synthesizer

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- Musical keyboard – controls VCO frequency, triggers envelopes.
- Knobs, switches, control inputs – set the synthesis parameters, introduce modulation.
- Pitch bender – a wheel to modulate pitch.
- Modulation wheel – can be assigned to any parameter, modulation by hand.
- Foot controllers.
- Controlling with computers (MIDI, only digital instruments).





# Types of subtractive synthesizers

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- **Monophonic** – only one sound (voice) at a time (the last pressed key or the highest key). In order to compensate for monophony, a large number of VCOs (e.g. 16) have to be used. Example: Moog Modular.
- **Polyphonic** – duplicated synthesis pipelines allow for generating multiple voices at a time and playing chords. Two or three VCOs are usually sufficient.

All modern subtractive synthesizers are polyphonic (but they usually can be switched to mono mode if a musician wishes so).

# Commercial subtractive instruments

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- Robert Moog's synthesizers – Moog Modular, MiniMoog, PolyMoog and others.
- ARP, Buchla, Oberheim, Sequential Circuits Prophet, Yamaha CS, Roland, Korg MS & PS.
- Later models from 1980s were hybrid synthesizers with digital oscillators (e.g. Roland Juno).
- Digital instruments (emulators) – e.g. Clavia Nord Lead 2X), “virtual analog synthesis”.
- Software synthesizers (VST) – a large number, including Arturia Moog Modular and free Synth1.

# Robert Moog with his “children”

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# Digital implementation of subtractive s.

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Subtractive synthesis may be implemented in digital as:

- hardware – instruments with keyboard, “virtual analog”, often combined with sampling and other methods,
- software – programs running on a computer; usually created in VSTi technology (need a VST host)
- modular software – a user builds the synthesis algorithm by connecting blocks (oscillators, modulators, etc.).



# Problems of digital implementation

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It's easy to create a digital subtractive synthesizer.

But it's very hard to make it sound good!

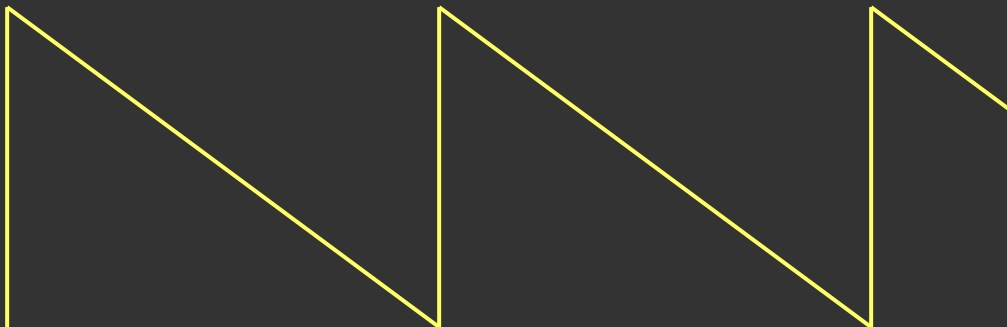
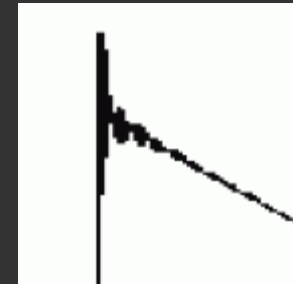
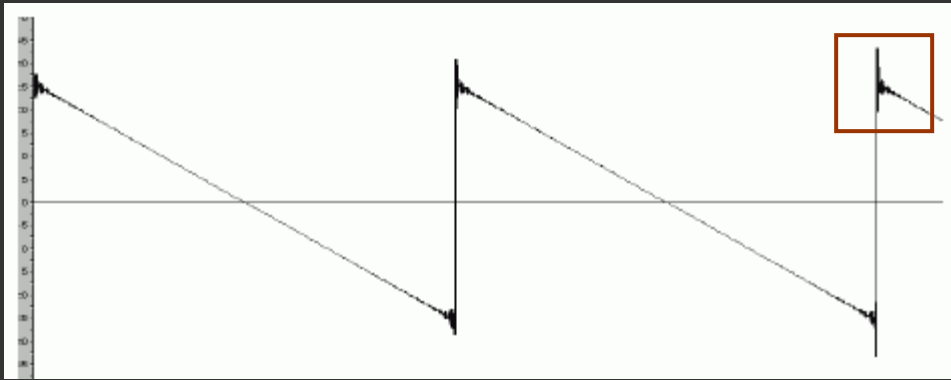
Digital devices are simply “too perfect”.

- Emulating imperfections of analogue synthesizers:
  - unstable wave shapes,
  - unstable parameters (but the frequency must be stable!)
- Digital oscillators – the aliasing problem.
- Differences in characteristics of analogue and digital filters.
- Level limiting (soft clipping).

# Problems of digital implementation

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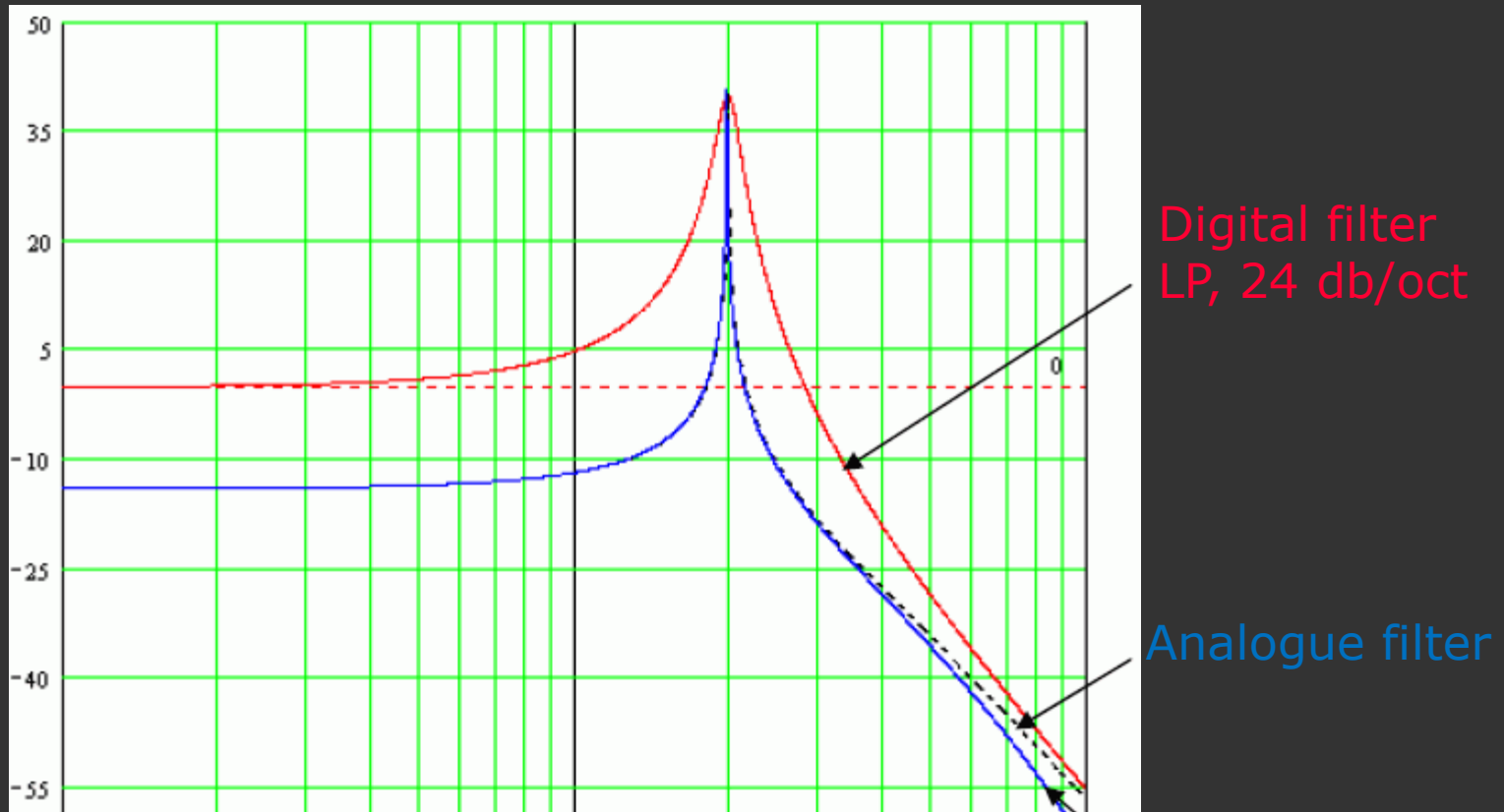
A sawtooth wave produced by Moog Modular vs. the ideal wave:





# Problems of digital implementation

## Transfer functions of resonant VCFs





# Summary

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## Pros:

- ability to create new interesting sounds
- novel sounds (unlike all instruments before)
- easy method to implement

## Cons:

- difficult to operate, many parameters to adjust
- it cannot replicate real instrument sounds
- problems with digital emulation
- analogue oscillators were unstable, they often detuned by themselves
- analogue instruments were expensive

# Bibliography

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- <http://moogarchives.com>  
Moog Archive – database of Robert Moog instruments
- <http://daichilab.com/synth1/>  
free software synthesizer Synth1
- <https://multimed.org/student/eim/doc/Synth1.pdf>  
Synth1 documentation
- <http://www.xs4all.nl/~rhordijk/G2Pages/>  
G2 Workshop - G2 synthesizer programming, subtractive synthesis theory
- <https://www.youtube.com/user/DoKashiteru>  
movies showing the work with Moog Modular